

JEE ADVANCED | JEE MAIN | NEET | OLYMPIADS | MHT-CET | FOUNDATION

29-Jan.-2024 (Evening) : PCM

MATHEMATICS Section - A (Single Correct Answer)

1. Let $A = \begin{bmatrix} 2 & 1 & 2 \\ 6 & 2 & 11 \\ 3 & 3 & 2 \end{bmatrix}$ and $P = \begin{bmatrix} 1 & 2 & 0 \\ 5 & 0 & 2 \\ 7 & 1 & 5 \end{bmatrix}$. The sum of the prime factors of $|P^{-1}AP - 21|$ is equal to (A) 26 (B) 27 (C) 66 (D) 23

Number of ways of arranging 8 identical books into 4 identical shelves where any number of shelves may remain empty is equal to

- (A) 18 (B) 16 (C) 12 (D) 15
- 3. Let P(3, 2, 3), Q(4, 6, 2) and R(7, 3, 2) be the vertices of \triangle PQR. Then, the angle \angle QPR is
 - (A) $\frac{\pi}{6}$ (B) $\cos^{-1}\left(\frac{7}{18}\right)$ (C) $\cos^{-1}\left(\frac{1}{18}\right)$ (D) $\frac{\pi}{3}$

4. If the mean and variance of five observations are $\frac{24}{5}$ and $\frac{194}{25}$ respectively and the mean of first four

observations is $\frac{7}{2}$, then the variance of the first four observations in equal to

(A) $\frac{4}{5}$ (B) $\frac{77}{12}$ (C) $\frac{5}{4}$ (D) $\frac{105}{4}$

5. The function $f(x) = 2x + 3(x)^{\frac{2}{3}}$, $x \in \mathbb{R}$, has

- (A) exactly one point of local minima and no point of local maxima
- (B) exactly one point of local maxima and no point of local minima
- (C) exactly one point of local maxima and exactly one point of local minima
- (D) exactly two points of local maxima and exactly one point of local minima
- 6. Let r and θ respectively be the modulus and amplitude of the complex number $z = 2 i\left(2\tan\frac{5\pi}{8}\right)$, then
 - (r, θ) is equal to

(A)
$$\left(2\sec\frac{3\pi}{8},\frac{3\pi}{8}\right)$$
 (B) $\left(2\sec\frac{3\pi}{8},\frac{5\pi}{8}\right)$ (C) $\left(2\sec\frac{5\pi}{8},\frac{3\pi}{8}\right)$ (D) $\left(2\sec\frac{11\pi}{8},\frac{11\pi}{8}\right)$

- 7. The sum of the solutions $x \in \mathbb{R}$ of the equations $\frac{3\cos 2x + \cos^3 2x}{\cos^6 x \sin^6 x} = x^3 x^2 + 6$ is
 - (A) 0 (B) 1
 - (C) -1 (D) 3



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17. Let
$$y = \log_e \left(\frac{1 - x^2}{1 + x^2} \right)$$
, $-1 < x < 1$. Then at $x = \frac{1}{2}$, the value of $225(y' - y'')$ is equal to
(A) 732 (B) 746 (C) 742 (D) 736

18. If R is the smallest equivalence relation on the set $\{1, 2, 3, 4\}$ such that $\{(1, 2), (1, 3)\} \subset R$, then the number of elements in R is_____

19. An integer is chosen at random from the integers 1, 2, 3, ..., 50. The probability that the chosen integer is a multiple of atleast one of 4, 6 and 7 is

(A)
$$\frac{8}{25}$$
 (B) $\frac{21}{50}$ (C) $\frac{9}{50}$ (D) $\frac{14}{25}$

20. Let a unit vector $\hat{\mathbf{u}} = \mathbf{x}\hat{\mathbf{i}} + \mathbf{y}\hat{\mathbf{j}} + \mathbf{z}\hat{\mathbf{k}}$ make angles $\frac{\pi}{2}$, $\frac{\pi}{3}$ and $\frac{2\pi}{3}$ with the vectors $\frac{1}{\sqrt{2}}\hat{\mathbf{i}} + \frac{1}{\sqrt{2}}\hat{\mathbf{k}}$, $\frac{1}{\sqrt{2}}\hat{\mathbf{j}} + \frac{1}{\sqrt{2}}\hat{\mathbf{k}}$

and
$$\frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{j}$$
 respectively. If $\vec{v} = \frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{j} + \frac{1}{\sqrt{2}}\hat{k}$, then $|\hat{u} - \vec{v}|^2$ is equal to
(A) $\frac{11}{2}$ (B) $\frac{5}{2}$ (C) 9 (D) 7

Section - B (Numerical Value Type)

21. Let α , β be teroots of the equation $x^2 - \sqrt{6}x + 3 = 0$ such that $Im(\alpha) > Im(\beta)$. Let a, b be integers not divisible by 3 and n be a natural number such that $\frac{\alpha^{99}}{\beta} + \alpha^{98} = 3^n (a + ib)$, $i = \sqrt{-1}$. Then n + a + b is equal to .

22. Let for any three distinct consecutive terms a, b, c of an A.P, the lines ax + by + c = 0 be concurrent at the point P and Q(α , β) be a point such that the system of equations x + y + z = 6, $2x + 5y + \alpha z = \beta$ and x + 2y + 3z = 4, has infinitely many solutions.

Then (PQ)² is equal to_____

23. Let P(α , β) be a point on the parabola $y^2 = 4x$. If P also lies on the chord of the parabola $x^2 = 8y$ whose mid point is $\left(1, \frac{5}{4}\right)$. Then ($\alpha - 28$) ($\beta - 8$) is equal to _____.

24. If
$$\int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \sqrt{1 - \sin 2x} \, dx = \alpha + \beta \sqrt{2} + \gamma \sqrt{3}$$
, where α , β and γ are are rational numbers, then $3\alpha + 4\beta - \gamma$ is equal to

25. Let the area of the region $\{(x, y): 0 \le x \le 3, 0 \le y \le \min\{x^2 + 2, 2x + 2\}\}$ be A. Then 12A is equal to



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26. Let O be the origin, and M and N be the points on the lines

 $\frac{x-5}{4} = \frac{y-4}{1} = \frac{z-5}{3} \text{ and } \frac{x+8}{12} = \frac{y+2}{5} = \frac{z+11}{9} \text{ respectively such that MN is the shortest distance between}$

the given lines. Then $\overrightarrow{OM} \cdot \overrightarrow{ON}$ is equal to _____

27. Let
$$f(x) = \sqrt{\lim_{r \to x} \left\{ \frac{2r^2[(f(r))^2 - f(x)f(r)]}{r^2 - x^2} - r^3 e^{\frac{f(r)}{r}} \right\}}$$
 be differentiable in $(-\infty, 0) \cup (0, \infty)$ and $f(1) = 1$.

Then the value of ea, such that f(a) = 0, is equal to _____.

- 28. Remainder when $64^{32^{32}}$ is divided by 9 is equal to _____.
- 29. Let the set $C = \{(x, y) | x^2 2^y = 2023, x, y \in \mathbb{N}\}$. Then $\sum_{(x, y) \in C} (x + y)$ is equal to _____.
- 30. Let the slope of the line 45x + 5y + 3 = 0 be $27r_1 + \frac{9r_2}{2}$ for some $r_1, r_2 \in \mathbb{R}$.

Then
$$\lim_{x \to 3} \left(\int_{3}^{x} \frac{8t^2}{\frac{3r_2x}{2} - r_2x^2 - r_1x^3 - 3x} dt \right)$$
 is equal to _____

PHYSICS

Section - A (Single Correct Answer)

- 31. Two sources of light emit with a power of 200 W. The ratio of number of photons of visible light emitted by each source having wavelengths 300 nm and 500 nm respectively, will be :
 - (A) 1:5 (B) 1:3 (C) 5:3 (D) 3:5
- 32. The truth table for this given circuit is :



	А	В	Y		Α	В	Y		А	В	Y		Α	В	Y
(A)	0	0	1	(B)	0	0	0	(C)	0	0	0	(D)	0	0	1
	0	1	1		0	1	1		0	1	0		0	1	0
	1	0	1		1	0	0		1	0	0		1	0	1
	1	1	0		1	1	1		1	1	1		1	1	0

33. A physical quantity Q is found to depend on quantities a, b, c by the relation $Q = \frac{a^4b^3}{c^2}$. The percentage error in a, b and c are 3%, 4% and 5% respectively. Then, the percentage error in Q is : (A) 66% (B) 43% (C) 34% (D) 14%

34. In an a.c. circuit, voltage and current are given by : V = 100 sin (100 t) V and I = 100 sin (100 t + π/3) mA respectively. The average power dissipated in one cycle is :
(A) 5 W
(B) 10 W
(C) 2.5 W
(D) 25 W

 35. The temperature of a gas having 2.0×10^{25} molecules per cubic meter at 1.38 atm

 (Given, k = 1.38×10^{-23} JK⁻¹) is :

 (A) 500 K
 (B) 200 K
 (C) 100 K
 (D) 300 K

36. A stone of mass 900g is tied to a string and moved in a vertical circle of radius 1m making 10 rpm. The tension in the string, when the stone is at the lowest point is (if π² = 9.8 and g = 9.8 m/s²)
(A) 97 N
(B) 9.8 N
(C) 8.82 N
(D) 17.8 N

37. The bob of a pendulum was released from a horizontal position. The length of the pendulum is 10m. If it dissipates 10% of its initial energy against air resistance, the speed with which the bob arrives at the lowest point is : [Use, $g : 10 \text{ ms}^{-2}$]

(A)
$$6\sqrt{5} \text{ ms}^{-1}$$
 (B) $5\sqrt{6} \text{ ms}^{-1}$ (C) $5\sqrt{5} \text{ ms}^{-1}$ (D) $2\sqrt{5} \text{ ms}^{-1}$

38. If the distance between object and its two times magnified virtual image produced by a curved mirror is 15 cm, the focal length of the mirror must be :

- (A) 15 cm (B) -12 cm (C) -10 cm (D) 10/3 cm
- 39. Two particles X and Y having equal charges are being accelerated through the same potential difference. Thereafter they enter normally in a region of uniform magnetic field and describes circular paths of radii R_1 and R_2 respectively. The mass ratio of X and Y is :

(A)
$$\left(\frac{R_2}{R_1}\right)^2$$
 (B) $\left(\frac{R_1}{R_2}\right)^2$ (C) $\left(\frac{R_1}{R_2}\right)$ (D) $\left(\frac{R_2}{R_1}\right)$

40. In Young's double slit experiment, light from two identical sources are superimposing on a screen. The path difference between the two lights reaching at a point on the screen is $7\lambda/4$. The ratio of intensity of fringe at this point with respect to the maximum intensity of the fringe is :

41. A small liquid drop of radius R is divided into 27 identical liquid drops. If the surface tension is T, then the work done in the process will be :

(A)
$$8\pi R^2 T$$
 (B) $3\pi R^2 T$ (C) $1/8 \pi R^2 T$ (D) $4\pi R^2 T$

42. A bob of mass 'm' is suspended by a light string of length 'L'. It is imparted a minimum horizontal velocity at the lowest point A such that it just completes half circle reaching the top most position B. The ratio of

kinetic energies
$$\frac{(K.E.)_{A}}{(K.E.)_{B}}$$
 is :







(B)

(A) 3:2

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- 43. A wire of length L and radius r is clamped at one end. If its other end is pulled by a force F, its length increases by *l*. If the radius of the wire and the applied force both are reduced to half of their original values keeping original length constant, the increase in length will become.
 - (A) 3 times (B) 3/2 times
 - (C) 4 times (D) 2 times
- 44. A planet takes 200 days to complete one revolution around the Sun. If the distance of the planet from Sun is reduced to one fourth of the original distance, how many days will it take to complete one revolution ?
 (A) 25
 (B) 50
 (C) 100
 (D) 20

45. A plane electromagnetic wave of frequency 35 MHz travels in free space along the X-direction. At a particular point (in space and time) $\vec{E} = 9.6\hat{j}$ V/m. The value of magnetic field at this point is :

- (A) $3.2 \times 10^{-8} \hat{k} T$ (B) $3.2 \times 10^{-8} \hat{i} T$
- (C) $9.6\,\hat{j}T$ (D) $9.6\times10^{-8}\,\hat{k}T$
- 46. In the given circuit, the current in resistance R_3 is :



47. A particle is moving in a straight line. The variation of position 'x' as a function of time 't' is given as $x = (t^3 - 6t^2 + 20t + 15)$ m. The velocity of the body when its acceleration becomes zero is :

- (A) 4 m/s (B) 8 m/s (C) 10 m/s (D) 6 m/s
- 48. N moles of a polyatomic gas (f = 6) must be mixed with two moles of a monoatomic gas so that the mixture behaves as a diatomic gas. The value of N is :

49. Given below are two statements :

(A) 1 A

Statement I : Most of the mass of the atom and all its positive charge are concentrated in a tiny nucleus and the electrons revolve around it, is Rutherford's model.

Statement II : An atom is a spherical cloud of positive charges with electrons embedded in it, is a special case of Rutherford's model.

In the light of the above statements, choose the most appropriate from the options given below.

- (A) Both statement I and statement II are false
- (B) Statement I is false but statement II is true
- (C) Statement I is true but statement II is false
- (D) Both statement I and statement II are true
- 50. An electric field is given by $(6\hat{i}+5\hat{j}+3\hat{k})N/C$. The electric flux through a surface area $30\hat{i}$ m² lying in

(D)

60

YZ-plane (in SI unit) is :

(A) 90 (B) 150 (C) 180

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Section - B (Numerical Value Type)

51. Two metallic wires P and Q have same volume and are made up of same material. If their area of cross sections are in the ratio 4 : 1 and force F_1 is applied to P, an extension of Δl is produced. The force which is required to produce same extension in Q is F_2 .

The value of
$$\frac{F_1}{F_2}$$
 is _____

52. A horizontal straight wire 5 m long extending from east to west falling freely at right angle to horizontal component of earth's magnetic field 0.60×10^{-4} Wbm⁻².

The instantaneous value of emf induced in the wire when its velocity is 10 ms⁻¹ is _____ \times 10⁻³ V.

53. Hydrogen atom is bombarded with electrons accelerated through a potential different of V, which causes excitation of hydrogen atoms. If the experiment is being formed at T = 0 K.

The minimum potential difference needed to observe any Balmer series lines in the emission spectra will

be
$$\frac{\alpha}{10}$$
 V, where $\alpha =$ _____.

54. A charge of 4.0 μ C is moving with a velocity of 4.0 \times 10⁶ ms⁻¹ along the positive y-axis under a magnetic field \vec{B} of strength $(2\hat{k})T$. The force acting on the charge is $x\hat{i}N$.

The value of x is _____.

55. A simple harmonic oscillator has an amplitude A and time period 6π second.

Assuming the oscillation starts from its mean position, the time required by it to travel from x = A to

$$x = \frac{\sqrt{3}}{2}A$$
 will be $\frac{\pi}{x}s$, where $x =$ _____.

56. In the given figure, the charge stored in 6μ F capacitor, when points A and B are joined by a connecting wire is _____ μ C.



57. In a single slit diffraction pattern, a light of wavelength 6000 Å is used. The distance between the first and third minima in the diffraction pattern is found to be 3 mm when the screen in placed 50 cm away from slits.

The width of the slit is $__ \times 10^{-4}$ m.



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58. In the given circuit, the current flowing through the resistance 20 Ω is 0.3 A, while the ammeter reads 0.9 A. The value of R₁ is _____ Ω .



59. A particle is moving in a circle of radius 50 cm in such a way that at any instant the normal and tangential components of its acceleration are equal. If its speed at t = 0 is 4 m/s, the time taken to complete the first

revolution will be $\frac{1}{\alpha} \left[1 - e^{-2\pi} \right] s$, where $\alpha =$ _____.

60. A body of mass 5 kg moving with a uniform speed $3\sqrt{2}$ ms⁻¹ in X-Y plane along the line y = x + 4. The angular momentum of the particle about the origin will be _____ kg m²s⁻¹.

CHEMISTRY	Section - A	(Single Correct Answer)	

61. The ascending acidity order of the following H-atoms is

				H ₃ C		
		$HC \equiv C - H$	$H_2C = CH$	H ₃ C - C ·	$- (H) H_3C - CH_2 - (H)$	
			Ĥ	H ₃ C		
		А	В	С	D	
	(A)	C < D < B < A		(B)	A < B < C < D	
	(C)	A < B < D < C		(D)	D < C < B < A	
62.	Mate	ch List I with List II :				
		List I (Bio Polymer	·)		List II (Monomer)	
	Α.	Starch		I.	nucleotide	
	В.	Cellulose		II.	α-glucose	
	C.	Nucleic acid		III.	β-glucose	
	D.	Protein		IV.	α -amino acid	
	Choo	ose the correct answer f	rom the options	given below	:	
	(A)	A-II, B-I, C-III, D-IV	Ι	(B)	A-IV, B-II, C-I, D-III	
	(C)	A-I, B-III, C-IV, D-I	[(D)	A-II, B-III, C-I, D-IV	
63.	Mate	ch List I with List II :				
		List I (Compound)			List II (pK _a value)	
	Α.	Ethanol		I.	10.0	
	В.	Phenol		II.	15.9	
	C.	m-Nitrophenol		III.	7.1	
	D.	p-Nitrophenol		IV.	8.3	





Choose the correct answer from the options given below :

- (A) A-I, B-II, C-III, D-IV (B) A-IV, B-I, C-II, D-III
 - A-III, B-IV, C-I, D-II (D) A-II, B-I, C-IV, D-III

64. Which of the following reaction is correct ?

(C)



Choose the correct answer from the options given below :

- (A) A-II, B-III, C-I, D-IV
- (C) A-II, B-IV, C-III, D-I

- (B) A-I, B-III, C-II, D-IV
- (D) A-I, B-II, C-III, D-IV



70.On passing a gas, 'X', through Nessler's reagent, a brown precipitate is obtained. The gas 'X' is(A) H2S(B) CO2(C) NH3(D) Cl2

CHO

71. The product A formed in the following reaction is :



72. Identify the reagents used for the following conversion.



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- 76. The element having the highest first ionization enthalpy is
 - (A) Si (B) Al (C) N (D) C
- 77. Alkyl halide is converted into alkyl isocyanide by reaction with(A) NaCN(B) NH₄CN(C) KCN(D) AgCN
- 78. Which one of the following will show geometrical isomerism ?



79. Given below are two statements :

Statement I : Fluorine has most negative electron gain enthalpy in its group.

Statement II : Oxygen has least negative electron gain enthalpy in its group.

In the light of the above statements, choose the most appropriate from the options given below.

- (A) Both Statement I and Statement II are true
- (B) Statement I is true but Statement II is false
- (C) Both Statement I and Statement II are false
- (D) Statement I is false but Statement II is true
- 80. Anomalous behaviour of oxygen is due to its
 - (A) Large size and high electronegativity
 - (B) Small size and low electronegativity
 - (C) Small size and high electronegativity
 - (D) Large size and low electronegativity

Section - B (Numerical Value Type)

- 81. The total number of anti bonding molecular orbitals, formed from 2s and 2p atomic orbitals in a diatomic molecule is _____.
- 82. The oxidation number of iron in the compound formed during brown ring test for NO_3^- ion is _____.
- 83. The following concentrations were observed at 500 K for the formation of NH₃ from N₂ and H₂. At equilibrium : $[N_2] = 2 \times 10^{-2} \text{ M}$, $[H_2] = 3 \times 10^{-2} \text{ M}$ and $[NH_3] = 1.5 \times 10^{-2} \text{ M}$. Equilibrium constant for the reaction is _____.
- 84. Molality of 0.8 M H_2SO_4 solution (density 1.06 g cm⁻³) is _____ × 10⁻³ m.
- If 50 mL of 0.5 M oxalic acid is required to neutralise 25 mL of NaOH solution, the amount of NaOH in 50 mL of given NaOH solution is _____ g.



- 86. The total number of 'Sigma' and Pi bonds in 2-formylhex-4-enoic acid is _____
- 87. The half-life of radioisotopic bromine 82 is 36 hours. The fraction which remains after one day is $___ \times 10^{-2}$.

[**Given :** antilog 0.2006 = 1.587]

- 88. Standard enthalpy of vapourisation for CCl₄ is 30.5 kJ mol⁻¹. Heat required for vapourisation of 284 g of CCl₄ at constant temperature is _____ kJ.
 [Civen molon model is a mole] is C = 12. Cl = 25. 51.
 - [Given molar mass in g mol⁻¹; C = 12, Cl = 35.5]
- 89. A constant current was passed through a solution of $AuCl_4^-$ ion between gold electrodes. After a period of 10.0 minutes, the increase in mass of cathode was 1.314 g. The total charge passed through the solution is _____ × 10⁻² F.

[Given atomic mass of Au = 197]

- 90. The total number of molecules with zero dipole moment among CH₄, BF₃, H₂O, HF, NH₃, CO₂ and SO₂ is _____.
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29-Jan.-2024 (Evening) : PCM

MATHEMATICS

Single	Choice	Correct								
	1.	А	2.	D	3.	D	4.	С	5.	С
	6.	А	7.	С	8.	D	9.	А	10.	D
	11.	D	12.	А	13.	D	14.	D	15.	D
	16.	В	17.	D	18.	А	19.	В	20.	В
Nume	rical Va	lue								
	21.	49	22.	113	23.	192	24.	6	25.	164
	26.	9	27.	2	28.	1	29.	46	30.	12

PHYSICS										
Single Choic	e Correct									
31.	D	32.	В	33.	С	34.	С	35.	А	
36.	В	37.	А	38.	С	39.	В	40.	А	
41.	А	42.	В	43.	D	44.	А	45.	А	
46.	А	47.	В	48.	С	49.	С	50.	С	
Numerical V	alue									
51.	16	52.	3	53.	121	54.	32	55.	2	
56.	36	57.	2	58.	30	59.	8	60.	60	

CHEMISTRY											
Single Choi	ce Correct										
61.	А	62.	D	63.	D	64.	В	65.	D		
66.	В	67.	D	68.	D	69.	С	70.	С		
71.	С	72.	D	73.	С	74.	С	75.	А		
76.	С	77.	D	78.	С	79.	D	80.	С		
Numerical	Value										
81.	4	82.	1	83.	417	84.	815	85.	4		
86.	22	87.	63	88.	56	89.	2	90.	3		

