## 12-April-2023 (Morning Batch): JEE Main Paper

## MATHEMATICS

Section - A (Single Correct Answer)

1. The number of five digit numbers, greater than 40000 and divisible by 5 , which can be formed using the digits $0,1,3,5,7$ and 9 without repetition, is equal to
(A) 120
(B) 132
(C) 72
(D) 96
2. Let $\alpha, \beta$ be the roots of the quadratic equation $x^{2}+\sqrt{6} x+3=0$. Then $\frac{\alpha^{23}+\beta^{23}+\alpha^{14}+\beta^{14}}{\alpha^{15}+\beta^{15}+\alpha^{10}+\beta^{10}}$ is equal to :
(A) 729
(B) 72
(C) 81
(D) 9
3. Let $<a_{n}>$ be a sequence such that $a_{1}+a_{2}+\ldots .+a_{n}=\frac{n^{2}+3 n}{(n+1)(n+2)}$. If $28 \sum_{k=1}^{10} \frac{1}{a_{k}}=p_{1} p_{2} p_{3} \ldots \ldots p_{m}$, where $\mathrm{p}_{1}, \mathrm{p}_{2}, \ldots . . \mathrm{p}_{\mathrm{m}}$ are the first m prime numbers, then m is equal to
(A) 7
(B) 6
(C) 5
(D) 8
4. Let the lines $l_{1}: \frac{\mathrm{x}+5}{3}=\frac{\mathrm{y}+4}{1}=\frac{\mathrm{z}-\alpha}{-2}$ and $l_{2}: 3 \mathrm{x}+2 \mathrm{y}+\mathrm{z}-2=0=\mathrm{x}-3 \mathrm{y}+2 \mathrm{z}-13$ be coplanar. If the point $\mathrm{P}(\mathrm{a}, \mathrm{b}, \mathrm{c})$ on $l_{1}$ is nearest to the point $\mathrm{Q}(-4,-3,2)$, then $|\mathrm{a}|+|\mathrm{b}|+|\mathrm{c}|$ is equal to
(A) 12
(B) 14
(C) 10
(D) 8
5. Let $\mathrm{P}\left(\frac{2 \sqrt{3}}{\sqrt{7}}, \frac{6}{\sqrt{7}}\right), \mathrm{Q}, \mathrm{R}$ and S be four points on the ellipse $9 \mathrm{x}^{2}+4 \mathrm{y}^{2}=36$. Let PQ and RS be mutually perpendicular and pass through the origin. If $\frac{1}{(P Q)^{2}}+\frac{1}{(R S)^{2}}=\frac{p}{q}$, where $p$ and $q$ are coprime, then $p+q$ is equal to
(A) 143
(B) 137
(C) 157
(D) 147
6. Let $a, b, c$ be three distinct real numbers, none equal to one. If the vectors $a \hat{i}+\hat{j}+\hat{k}, \hat{i}+b \hat{j}+\hat{k}$ and $\hat{\mathrm{i}}+\hat{\mathrm{j}}+\mathrm{c} \hat{\mathrm{k}}$ are coplanar, then $\frac{1}{1-\mathrm{a}}+\frac{1}{1-\mathrm{b}}+\frac{1}{1-\mathrm{c}}$ is equal to :
(A) 1
(B) -1
(C) -2
(D) 2
7. If the local maximum value of the function $f(x)=\left(\frac{\sqrt{3 e}}{2 \sin x}\right)^{\sin ^{2} x}, x \in\left(0, \frac{\pi}{2}\right)$, is $\frac{k}{e}$, then $\left(\frac{k}{e}\right)^{8}+\frac{k^{8}}{e^{5}}+k^{8}$ is equal to
(A) $e^{5}+e^{6}+e^{11}$
(B) $\mathrm{e}^{3}+\mathrm{e}^{5}+\mathrm{e}^{11}$
(C) $e^{3}+e^{6}+e^{11}$
(D) $e^{3}+e^{6}+e^{10}$
8. Let D be the domain of the function $\mathrm{f}(\mathrm{x})=\sin ^{-1}\left(\log _{3 x}\left(\frac{6+2 \log _{3} \mathrm{x}}{-5 \mathrm{x}}\right)\right)$. If the range of the function $\mathrm{g}: \mathrm{D}$ $\rightarrow R$ defined by $g(x)=x-[x]$, ([x] is the greatest integer function), is $[\alpha, \beta)$, then $\left[\alpha^{2}\right]+\frac{5}{\beta}$ is equal to
(A) 46
(B) 135
(C) 136
(D) 45
9. Let $\mathrm{y}=\mathrm{y}(\mathrm{x}), \mathrm{y}>0$, be a solution curve of the differential equation $\left(1+\mathrm{x}^{2}\right) \mathrm{dy}=\mathrm{y}(\mathrm{x}-\mathrm{y}) \mathrm{dx}$. If $\mathrm{y}(0)=1$ and $y(2 \sqrt{2})=\beta$, then
(A) $\mathrm{e}^{3 \beta^{-1}}=\mathrm{e}(3+2 \sqrt{2})$
(B) $\mathrm{e}^{\beta^{-1}}=\mathrm{e}^{-2}(5+\sqrt{2})$
(C) $\mathrm{e}^{\mathrm{\beta}^{-1}}=\mathrm{e}^{-2}(3+2 \sqrt{2})$
(D) $\mathrm{e}^{3 \beta^{-1}}=\mathrm{e}(5+\sqrt{2})$
10. Among the two statements
$(\mathrm{Sl}):(\mathrm{p} \rightarrow \mathrm{q}) \wedge(\mathrm{q} \wedge(\sim \mathrm{q}))$ is a contradiction and
$(S 2):(p \wedge q) \vee((\sim \mathrm{p}) \wedge \mathrm{q}) \vee(\mathrm{p} \wedge(\sim \mathrm{q})) \vee((\sim \mathrm{p}) \wedge(\sim \mathrm{q}))$ is a tautology
(A) only (S2) is true
(B) only (S1) is true
(C) both are false
(D) both are true
11. Let $\lambda \in Z, \vec{a}=\lambda \hat{i}+\hat{j}-\hat{k}$ and $\vec{b}=3 \hat{i}-\hat{j}+2 \hat{k}$. Let $\vec{c}$ be a vector such that $(\vec{a}+\vec{b}+\vec{c}) \times \vec{c}=\overrightarrow{0}, \vec{a} \cdot \vec{c}=-17$ and $\vec{b} \cdot \vec{c}=-20$. Then $|\vec{c} \times(\lambda \hat{i}+\hat{j}+\hat{k})|^{2}$ is equal to :
(A) 62
(B) 46
(C) 53
(D) 49
12. The sum of the coefficients of the first 50 terms in the binomial expansion of $(1-x)^{100}$ is equal to
(A) $-{ }^{101} \mathrm{C}_{50}$
(B) ${ }^{99} \mathrm{C}_{49}$
(C) $-{ }^{99} \mathrm{C}_{49}$
(D) ${ }^{101} \mathrm{C}_{50}$
13. The area of the region enclosed by the curve $y=x^{3}$ and its tangent at the point $(-1,-1)$ is
(A) $\frac{27}{4}$
(B) $\frac{19}{4}$
(C) $\frac{23}{4}$
(D) $\frac{31}{4}$
14. Let $\mathrm{A}=\left[\begin{array}{cc}1 & \frac{1}{51} \\ 0 & 1\end{array}\right]$. If $\mathrm{B}=\left[\begin{array}{cc}1 & 2 \\ -1 & -1\end{array}\right] \mathrm{A}\left[\begin{array}{cc}-1 & -2 \\ 1 & 1\end{array}\right]$, then the sum of all the elements of the matrix $\sum_{\mathrm{n}=1}^{50} \mathrm{~B}^{\mathrm{n}}$ is equal to :
(A) 100
(B) 50
(C) 75
(D) 125
15. Let the plane $P: 4 x-y+z=10$ be rotated by an angle $\frac{\pi}{2}$ about its line of intersection with the plane $x+$ $y-z=4$. If $\alpha$ is the distance of the point $(2,3,-4)$ from the new position of the plane $P$, then $35 \alpha$ is
(A) 90
(B) 85
(C) 105
(D) 126
16. If $\frac{1}{\mathrm{n}+1}{ }^{\mathrm{n}} \mathrm{C}_{\mathrm{n}}+\frac{1}{\mathrm{n}}{ }^{\mathrm{n}} \mathrm{C}_{\mathrm{n}-1}+\ldots .+\frac{1}{2}{ }^{\mathrm{n}} \mathrm{C}_{1}+{ }^{\mathrm{n}} \mathrm{C}_{0}=\frac{1023}{10}$ then n is equal to
(A) 6
(B) 9
(C) 8
(D) 7
17. Let C be the circle in the complex plane with centre $\mathrm{z}_{0}=\frac{1}{2}(1+3 \mathrm{i})$ and radius $\mathrm{r}=1$. Let $\mathrm{z}_{1}=1+\mathrm{i}$ and the complex number $\mathrm{z}_{2}$ be outside the circle C such that $\left|\mathrm{z}_{1}-\mathrm{z}_{0}\right|\left|\mathrm{z}_{2}-\mathrm{z}_{0}\right|=1$. If $\mathrm{z}_{0}, \mathrm{z}_{1}$ and $\mathrm{z}_{2}$ are collinear, then the smaller value of $\left|z_{2}\right|^{2}$ is equal to
(A) $\frac{13}{2}$
(B) $\frac{5}{2}$
(C) $\frac{3}{2}$
(D) $\frac{7}{2}$
18. If the point $\left(\alpha, \frac{7 \sqrt{3}}{3}\right)$ lies on the curve traced by the mid-points of the line segments of the lines $\mathrm{x} \cos \theta+\mathrm{y} \sin \theta=7, \theta \in\left(0, \frac{\pi}{2}\right)$ between the co-ordinates axes, then $\alpha$ is equal to
(A) 7
(B) -7
(C) $-7 \sqrt{3}$
(D) $7 \sqrt{3}$
19. Two dice $A$ and $B$ are rolled. Let the numbers obtained on $A$ and $B$ be $\alpha$ and $\beta$ respectively. If the variance of $\alpha-\beta$ is $\frac{p}{q}$, where $p$ and $q$ are co-prime, then the sum of the positive divisors of $p$ is equal to
(A) 36
(B) 48
(C) 31
(D) 72
20. In a triangle ABC , if $\cos \mathrm{A}+2 \cos \mathrm{~B}+\cos \mathrm{C}=2$ and the lengths of the sides opposite to the angles A and C are 3 and 7 respectively, then $\cos \mathrm{A}-\cos \mathrm{C}$ is equal to
(A) $\frac{3}{7}$
(B) $\frac{9}{7}$
(C) $\frac{10}{7}$
(D) $\frac{5}{7}$

## SECTION - B

21. A fair $n(n>1)$ faces die is rolled repeatedly until a number less than $n$ appears. If the mean of the number of tosses required is $\frac{n}{9}$, then $n$ is equal to $\qquad$ .
22. Let the digits $\mathrm{a}, \mathrm{b}, \mathrm{c}$ be in A.P. Nine-digit numbers are to be formed using each of these three digits thrice such that three consecutive digits are in A.P. at least once. How many such numbers can be formed ?
23. Let $[x]$ be the greatest integer $\leq x$. Then the number of points in the interval $(-2,1)$, where the function $f(x)=|[x]|+\sqrt{x-[x]}$ is discontinuous is $\qquad$ .
24. Let the plane $x+3 y-2 z+6=0$ meet the co-ordinate axes at the points $A, B, C$. If the orthocentre of the triangle ABC is $\left(\alpha, \beta, \frac{6}{7}\right)$, then $98(\alpha+\beta)^{2}$ is equal to $\qquad$ -
25. Let $I(x)=\int \sqrt{\frac{x+7}{x}} d x$ and $I(9)=12+7 \log _{e} 7$. If $I(1)=\alpha+7 \log _{e}(1+2 \sqrt{2})$, then $\alpha^{4}$ is equal to $\qquad$ .
26. Let $D_{k}=\left|\begin{array}{ccc}1 & 2 k & 2 k-1 \\ n & n^{2}+n+2 & n^{2} \\ n & n^{2}+n & n^{2}+n+2\end{array}\right|$. If $\sum_{k=1}^{n} D_{k}=96$, then $n$ is equal to
27. Let the positive numbers $\mathrm{a}_{1}, \mathrm{a}_{2}, \mathrm{a}_{3}, \mathrm{a}_{4}$ and $\mathrm{a}_{5}$ be in a G.P. Let their mean and variance be $\frac{31}{10}$ and $\frac{\mathrm{m}}{\mathrm{n}}$ respectively, where $m$ and $n$ are co-prime. If the mean of their reciprocals is $\frac{31}{40}$ and $a_{3}+a_{4}+a_{5}=14$, then $m+n$ is equal to $\qquad$ .
28. The number of relations, on the set $\{1,2,3\}$ containing $(1,2)$ and $(2,3)$, which are reflexive and transitive but not symmetric, is $\qquad$
29. If $\int_{-0.15}^{0.15}\left|100 x^{2}-1\right| d x=\frac{k}{3000}$, then $k$ is equal to $\qquad$ .
30. Two circles in the first quadrant of radii $r_{1}$ and $r_{2}$ touch the coordinate axes. Each of them cuts off an intercept of 2 units with the line $x+y=2$. Then $r_{1}^{2}+r_{2}^{2}-r_{1} r_{2}$ is equal to $\qquad$ _.

## PHYSICS

## Section - A (Single Correct Answer)

31. An ice cube has a bubble inside. When viewed from one side the apparent distance of the bubble is 12 cm . when viewed from the opposite side, the apparent distance of the bubble is observed as 4 cm . If the side of the ice cube is 24 cm , the refractive index of the ice cube is
(A) $4 / 3$
(B) $3 / 2$
(C) $2 / 3$
(D) $6 / 5$
32. Two satellites $A$ and $B$ move round the earth in the same orbit. The mass of $A$ is twice the mass of $B$. The quantity which is same for the two satellites will be :
(A) Potential energy
(B) Total energy
(C) Kinetic energy
(D) Speed
33. The amplitude of $15 \sin (1000 \pi t)$ is modulated by $10 \sin (4 \pi t)$ signal. The amplitude modulated signal contains frequencies of
34. 500 Hz .
35. 2 Hz
36. 250 Hz
37. 498 Hz
38. 502 Hz

Choose the correct answer from the options given below:
(A) (1) and (3) only
(B) (1) and (4) only
(C) (1) and (2) only
(D) (1), (4) and (5) only
34. In an n-p-n common emitter (CE) transistor the collector current changes from 5 mA to 16 mA for the change in base current from $100 \mu \mathrm{~A}$ and $200 \mu \mathrm{~A}$, respectively. The current gain of transistor is $\qquad$ -.
(A) 110
(B) 0.9
(C) 210
(D) 9
35. If the r.m.s. speed of chlorine molecule is $490 \mathrm{~m} / \mathrm{s}$ at $27^{\circ} \mathrm{C}$, the r.m.s. speed of argon molecules at the same temperature will be (Atomic mass of argon $=39.9 \mathrm{u}$, molecular mass of chlorine $=70.9 \mathrm{u}$ )
(A) $751.7 \mathrm{~m} / \mathrm{s}$
(B) $451.7 \mathrm{~m} / \mathrm{s}$
(C) $651.7 \mathrm{~m} / \mathrm{s}$
(D) $551.7 \mathrm{~m} / \mathrm{s}$
36. A proton and an $\alpha$-particle are accelerated from rest by 2 V and 4 V potentials, respectively. The ratio of their de-Broglie wavelength is:
(A) $4: 1$
(B) $2: 1$
(C) $8: 1$
(D) $16: 1$
37. Given below are two statements:

Statement I : The diamagnetic property depends on temperature.
Statement II : The included magnetic dipole moment in a diamagnetic sample is always opposite to the magnetizing field.

In the light of given statement, choose the correct answer from the options given below:
(A) Statement I is incorrect but Statement II is true
(B) Both Statement I and Statement II are true.
(C) Both Statement I and Statement II are false.
(D) Statement I is correct but Statement II is false.
38. A wire of resistance $160 \Omega$ is melted and drawn in wire of one-fourth of its length. The new resistance of the wire will be
(A) $10 \Omega$
(B) $640 \Omega$
(C) $40 \Omega$
(D) $16 \Omega$
39. Match List I with List II

## List I

A. Spring constant
B. Angular speed
C. Angular momentum
D. Moment of Inertia

## List II

I. $\quad\left(\mathrm{T}^{-1}\right)$
II. $\left(\mathrm{MT}^{-2}\right)$
III. $\left(\mathrm{ML}^{2}\right)$
IV. $\quad\left(\mathrm{ML}^{2} \mathrm{~T}^{-1}\right)$

Choose the correct answer from the options given below:
(A) A-II, B-I, C-IV, D-III
(B) A-IV, B-I, C-III, D-II
(C) A-II, B-III, C-I, D-IV
(D) A-I, B-III, C-II, D-IV
40. Three force $\mathrm{F}_{1}=10 \mathrm{~N}, \mathrm{~F}_{2}=8 \mathrm{~N}, \mathrm{~F}_{3}=6 \mathrm{~N}$ are acting on a particle of mass 5 kg . The forces $\mathrm{F}_{2}$ and $\mathrm{F}_{3}$ are applied perpendicular so that particle remains at rest. If the force $\mathrm{F}_{1}$ is removed, then the acceleration of the particle is:
(A) $2 \mathrm{~ms}^{-2}$
(B) $0.5 \mathrm{~ms}^{-2}$
(C) $4.8 \mathrm{~ms}^{-2}$
(D) $7 \mathrm{~ms}^{-2}$
41. A body cools from $80^{\circ} \mathrm{C}$ to $60^{\circ} \mathrm{C}$ in 5 minutes. The temperature of the surrounding is $20^{\circ} \mathrm{C}$. The time it takes to cool from $60^{\circ} \mathrm{C}$ to $40^{\circ} \mathrm{C}$ is:
(A) 500 s
(B) $\frac{25}{3} \mathrm{~s}$
(C) 450 s
(D) 420 s
42. An engine operating between the boiling and freezing points of water will have

1. efficiency more than $27 \%$
2. efficiency less than the efficiency a Carnot engine operating between the same two temperatures.
3. efficiency equal to $27 \%$
4. efficiency less than $27 \%$
(A) 2, 3 and 4 only
(B) 2 and 3 only
(C) 2 and 4 only
(D) 1 and 2 only
5. Given below are two statements:

Statement I : A truck and a car moving with same kinetic energy are brought to rest by applying brakes which provide equal retarding forces. Both come to rest in equal distance.
Statement II : A car moving towards east takes a turn and moves towards north, the speed remains unchanged. The acceleration of the car is zero.
In the light of given statements, choose the most appropriate answer from the options given below.
(A) Statement I is correct but Statement II is incorrect
(B) Statement I is incorrect but Statement II is correct
(C) Both Statement I is correct but Statement II are incorrect
(D) Both Statement I is correct but Statement II are correct
44. A particle is executing Simple Harmonic Motion (SHM). The ratio of potential energy and kinetic energy of the particle when its displacement is half of its amplitude will be:
(A) $1: 1$
(B) $2: 1$
(C) $1: 4$
(D) $1: 3$
45. A ball is thrown vertically upward with an initial velocity of $150 \mathrm{~m} / \mathrm{s}$. The ratio of velocity after 3 s and 5 s is $\frac{x+1}{x}$. The value of $x$ is $\qquad$ . Take ( $\mathrm{g}=10 \mathrm{~m} / \mathrm{s}^{2}$ ).
(A) 6
(B) 5
(C) $\quad-5$
(D) 10
46. Given below are two statement: one is labelled as Assertion $\mathbf{A}$ and the other is labelled as Reason R.

Assertion A : If an electric dipole of dipole moment $30 \times 10^{-5} \mathrm{Cm}$ is enclosed by a closed surface, the net flux coming out of the surface will be zero.
Reason $\mathbf{R}$ : Electric dipole consists of two equal and opposite charges.
In the light of above, statements, choose the correct answer from the options given below:
(A) Both $\mathbf{A}$ and $\mathbf{R}$ are true and $\mathbf{R}$ is the correct explanation of $\mathbf{A}$
(B) $\mathbf{A}$ is true but $\mathbf{R}$ is false
(C) Both $\mathbf{A}$ and $\mathbf{R}$ true but $\mathbf{R}$ is NOT the correct explanation of $\mathbf{A}$
(D) $\mathbf{A}$ is false but $\mathbf{R}$ is true
47. Given below are two statement : one is labelled as Assertion A and the other is labelled as Reason R.

Assertion A : EM waves used for optical communication have longer wavelengths than that of microwave, employed in Radar technology.
Reason R : Infrared EM waves are more energetic than microwaves, (used in Radar)
In the light of given statements, choose the correct answer from the options given below:
(A) $\mathbf{A}$ is false but $\mathbf{R}$ is true
(B) $\mathbf{A}$ is true but $\mathbf{R}$ is false
(C) Both $\mathbf{A}$ and $\mathbf{R}$ true but $\mathbf{R}$ is NOT the correct explanation of $\mathbf{A}$
(D) Both $\mathbf{A}$ and $\mathbf{R}$ true and $\mathbf{R}$ is the correct explanation of $\mathbf{A}$
48. A 12.5 eV electron beam is used to bombard gaseous hydrogen at room temperature. The number of spectral lines emitted will be:
(A) 2
(B) 1
(C) 3
(D) 4
49. The ratio of escape velocity of a planet to the escape velocity of earth will be:

Given : Mass of the planet is 16 times mass of earth and radius of the planet is 4 times the radius of earth.
(A) $4: 1$
(B) $2: 1$
(C) $1: 2$
(D) $1: 4$
50. Given below are two statements :

Statement I: When the frequency of an a.c. source in a series LCR circuit increases, the current in the circuit first increases, attains a maximum value and then decreases.
Statement II : In a series LCR circuit, the value of power factor at resonance is one.
In the light of given statements, choose the most appropriate answer from the options given below:
(A) Statement I is incorrect but Statement II is true.
(B) Both Statement I and Statement II are false.
(C) Statement I is correct but Statement II is false.
(D) Both Statement I and Statement II are true.

## SECTION - B

51. For a certain organ pipe, the first three resonance frequencies are in the ratio of $1: 3: 5$ respectively. If the frequency of fifth harmonic is 405 Hz and the speed of sound in air is $324 \mathrm{~ms}^{-1}$ the length of the organ pipe is $\qquad$ m.
52. For a rolling spherical shell, the ratio of rotational kinetic energy and total kinetic energy is $x / 5$. The value of x is $\qquad$ .
53. A compass needle oscillates 20 times per minute at a place where the dip is $30^{\circ}$ and 30 times per minute where the dip is $60^{\circ}$. The ratio of total magnetic field due to the earth at two place respectively is $\frac{4}{\sqrt{\mathrm{x}}}$. The value of $x$ is
54. A conducting circular loop is placed in a uniform magnetic field of 0.4 T with its plane perpendicular to the field. Somehow, the radius of the loop starts expanding at a constant rate of $1 \mathrm{~mm} / \mathrm{s}$. The magnitude of induced emf in the loop at an instant when the radius of the loop is 2 cm will be $\qquad$ $\mu \mathrm{V}$.
55. To maintain a speed of $80 \mathrm{~km} / \mathrm{h}$ by a bus of mass 500 kg on a plane rough road for 4 km distance, the work done by the engine of the bus will be $\qquad$ KJ. [The coefficient of friction between tyre of bus and road is 0.04 ].
56. A common example of alpha decay is ${ }_{92}^{238} \mathrm{U} \longrightarrow{ }_{90}^{234} \mathrm{Th}+{ }_{2} \mathrm{He}^{4}+\mathrm{Q}$

Given : ${ }_{92}^{238} \mathrm{U}=238.05060 \mathrm{u},{ }_{90}^{234} \mathrm{Th}=234.04360 \mathrm{u},{ }_{2}^{4} \mathrm{He}=4.00260 \mathrm{u}$, and $1 \mathrm{u}=931.5 \frac{\mathrm{MeV}}{\mathrm{c}^{2}}$
The energy released (Q) during the alpha decay of ${ }_{92}^{238} \mathrm{U}$ is $\qquad$ MeV
57. The current flowing through a conductor connected across a source is 2 A and 1.2 A at $0^{\circ} \mathrm{C}$ and $100^{\circ} \mathrm{C}$ respectively. The current flowing through the conductor at $50^{\circ} \mathrm{C}$ will be $\qquad$ $\times 10^{2} \mathrm{~mA}$.
58. Two convex lenses of focal length 20 cm each are placed coaxially with a separation of 60 cm between them. The image of the distant object formed by the combination is at $\qquad$ cm from the first lens.
59. Glycerine of density $1.25 \times 10^{3} \mathrm{~kg} \mathrm{~m}^{-3}$ is flowing through the conical section of pipe. The area of crosssection of the pipe at its ends is $10 \mathrm{~cm}^{2}$ and $5 \mathrm{~cm}^{2}$ and pressure drop across its length is $3 \mathrm{Nm}^{-2}$. The rate of flow of glycerine through the pipe is $x \times 10^{-5} \mathrm{~m}^{3} \mathrm{~s}^{-1}$. The value of x is $\qquad$ -.
60. 64 identical drops each charged upto potential of 10 mV are combined to form a bigger dorp. The potential of the bigger drop will be $\qquad$ mV .

## CHEMISTRY

61. 


(A)

(B)

(C)

(D)

62. Four gases A, B, C and D have critical temperatures 5.3, 33.2, 126.0 and 154.3 K respectively.

For their adsorption on fixed amount of charcoal, the correct order is :
(A) C $>$ B $>$ D $>$ A
(B) C $>$ D $>$ B $>$ A
(C) D $>$ C $>$ A $>$ B
(D) D $>$ C $>$ B $>$ A
63. Given below are two statement: one is labelled as Assertion A and the other is labelled as Reason $\mathbf{R}$ Assertion A: 5 f electrons can participate in bonding to a far greater extent than $4 f$ electrons
Reason R: 5f orbitals are not as buried as 4 f orbitals
In the light of the above statements, choose the correct answer from the options given below
(A) Both A and R are true but R is NOT the correct explanation of A
(B) Both A and R are true and R is the correct explanation of A
(C) A is false but R is true
(D) A is true but R is
64. The incorrect statement regarding the reaction given below is

(A) The electrophile involved in the reaction is $\mathrm{NO}^{+}$
(B) ' B ' is N -nitroso ammonium compound
(C) The reaction occurs at low temperature
(D) The product ' B ' formed in the above reaction is p -nitroso compound at low temperature
65. Match List I with List II

## LIST I Complex $\quad$ LIST II CFSE $\left(\Delta_{0}\right)$

A. $\left[\mathrm{Cu}\left(\mathrm{NH}_{3}\right) 6\right]^{2+}$ I. -0.6
B. $\left[\mathrm{Ti}\left(\mathrm{N}_{2} \mathrm{O}\right)_{6}\right]^{3+}$
II. -2.0
C. $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{3}$
III. -1.2
D. $\left[\mathrm{NIF}_{6}\right]^{4}$
IV. -0.4

Choose the correct answer from the options given below :
(A) A-I, B-IV, C-II, D-III
(B) A-II, B-III, C-I, D-IV
(C) A-I, B-II, C-IV, D-III
(D) A-III, B-IV, C-I, D-II
66. Match List I with List II

LIST I
(Examples)
A. 2-Chloro-1, 3 - butadiene
B. Nylon 2-nylon 6
C. Polyacrylonitrile
D. Dacron
I. Biodegradable polymer

LIST I
(Examples)
II. Synthetic Rubber
III. Polyester
IV. Addition Polymer

Choose the correct answer from the options given below :
(A) A-IV, B-I, C-III, D-II
(B) A-IV, B-III, C-I, D-II
(C) A-II, B-IV, C-I, D-III
(D) A-II, B-I, C-IV, D-III
67. The density of alkali metals is in the order
(A) $\mathrm{Na}<\mathrm{K}<\mathrm{Cs}<\mathrm{Rb}$
(B) $\mathrm{K}<\mathrm{Na}<\mathrm{Rb}<\mathrm{Cs}$
(C) $\mathrm{K}<\mathrm{Cs}<\mathrm{Na}<\mathrm{Rb}$
(D) $\mathrm{Na}<\mathrm{Rb}<\mathrm{K}<\mathrm{Cs}$
68. Given below are two statements :

Statements : $\mathrm{SbCl}_{5}$ is more covalent than $\mathrm{SbCl}_{3}$
Statements : The higher oxides of halogens also tend to be more stable than the lower ones.
In the light of the above statements, choose the most appropriate answer from the options given below
(A) Both statement I and Statement II are correct
(B) Both statement I and Statement II are incorrect
(C) Statement I is correct but Statement II is incorrect
(D) Statement I is incorrect but Statement II is correct
69. A metal chloride contains $55.0 \%$ of chlorine by weight. 100 mL vapours of the metal chloride at STP weigh 0.57 g . The molecular formula of the metal chloride is
(Given : Atomic mass of chlorine is 35.5 u )
(A) $\quad \mathrm{MCl}_{2}$
(B) $\mathrm{MCl}_{4}$
(C) $\quad \mathrm{MCl}_{3}$
(D) MCl
70. Given below are two statements : one is labelled as Assertion A and the other is labelled as Reason R Assertion A : In the Ellingham diagram, a sharp change in slope of the line is observed for $\mathrm{Mg} \rightarrow \mathrm{MgO}$ at $1120^{\circ} \mathrm{C}$
Reason $\mathbf{R}$ : There is a large change of entropy associated with the change of state In the light of the above statements, choose the correct answer from the options given below
(A) Both A and R are true but R is NOT the correct explanation of A
(B) Both A and R are true and R is the correct explanation of A
(C) A is false but R is true
(D) A is true but R is
71. Match List I with List II

|  | LIST I |  | LIST II |
| :--- | :--- | :--- | :--- |
| A. | Nitrogen oxides in air | I. | Eutrophication |
| B. | Methane in air | II. | pH of rain water becomes 5.6. |
| C. | Carbon dioxide | III. | Global warming |
| D. | Phosphate fertilisers in water | IV. | Acid rain |

Choose the correct answer from the options given below :
(A) A-IV, B-III, C-II, D-I
(B) A-II, B-III, C-I, D-IV
(C) A-I, B-II, C-III, D-IV
(D) A-IV, B-II, C-III, D-I
72. For lead storage battery pick the correct statements
A. During charging of battery, $\mathrm{PbSO}_{4}$ on anode is converted into $\mathrm{PbO}_{2}$
B. During charging of battery, $\mathrm{PbSO}_{4}$ on cathode is converted into $\mathrm{PbO}_{2}$
C. Lead storage battery, consists of grid of lead packed with $\mathrm{PbO}_{2}$ as anode
D. Lead storage battery has $\sim 38 \%$ solution of sulphuric acid as an electrolyte

Choose the correct answer from the options given below :
(A) B, D only
(B) B , C, D only
(C) A, B, D only
(D) B, C only
73. 2 -hexene $\xrightarrow[\text { (ii) } \mathrm{H}_{2} \mathrm{O}]{\text { (i) } \mathrm{O}_{3}}$ Product

The two products formed in above reaction are -
(A) Butanoic acid and acetic acid
(B) Butanal and acetic acid
(C) Butanal and acetaldehyde
(D) Butanoic acid and acetaldehyde
74. Correct statements for the given reaction are :

A. Compound ' B ' is aromatic
B. The completion of above reaction is very slow
C. 'A' shows tautomerism
D. The bond lengths $\mathrm{C}-\mathrm{C}$ in compound B are found to be same

Choose the correct answer from the options given below :
(A) A, B and D only
(B) A, B and C only
(C) B, C and D only
(D) A, C and D only
75. The bond order and magnetic property of acetylide ion are same as that of
(A) $\mathrm{NO}^{+}$
(B) $\mathrm{O}_{2}^{+}$
(C) $\mathrm{O}_{2}^{-}$
(D) $\mathrm{N}_{2}^{+}$
76. In the given reaction cycle

$\mathrm{X}, \mathrm{Y}$ and Z resppectively are
$\begin{array}{cccc} & \mathrm{X} & \mathrm{Y} & \mathrm{Z} \\ \text { (A) } & \mathrm{CaO} & \mathrm{NaCl}+\mathrm{CO}_{2} & \mathrm{KCl}\end{array}$
(B) $\begin{array}{ccc}\mathrm{X} & \mathrm{Y} & \mathrm{Z} \\ \mathrm{CaCO}_{3} & \mathrm{NaCl} & \mathrm{KCl}\end{array}$
(C) $\begin{array}{ccc}\mathrm{X} & \mathrm{Y} & \mathrm{Z} \\ \mathrm{CaCO}_{3} & \mathrm{NaCl} & \mathrm{KCl}\end{array}$
$\begin{array}{cccc} & \mathrm{X} & \mathrm{Y} & \mathrm{Z} \\ \text { (D) } & \mathrm{CaO} & \mathrm{NaCl}+\mathrm{CO}_{2} & \mathrm{NaCl}\end{array}$
77. Given below are two statements :

Statement I: Boron is extremely hard indicating its high lattice energy
Statement II : Boron has highest melting and boiling point compared to its other group members.
In the light of the above statements, choose the most appropriate answer from the options given below
(A) Statement I is incorrect but Statement II is correct
(B) Both Statement I and Statement II is correct
(C) Statement I is correct but Statement II is incorrect
(D) Both Statement I and Statement II is incorrect
78.


A in the above reaction is :
(A)

(B)

(C)

(D)

79. Match List I with List II

## LIST I Type of Hydride $\quad$ LIST II Example

A. Electron deficient hydride
I. $\mathrm{MgH}_{2}$
B. Electron rich hydride
II. HF
C. Electron precise hydride
III. $\quad \mathrm{B}_{2} \mathrm{H}_{6}$
D. Saline hydride
IV. $\mathrm{CH}_{4}$

Choose the correct answer from the options given below :
(A) A-III, B-II, C-IV, D-I
(B) A-II, B-III, C-IV, D-I
(C) A-II, B-III, C-I, D-IV
(D) A-III, B-II, C-I, D-IV
80. The major product ' P ' formed in the following sequence of reactions is


H
(A)

(B)

(C)

(D)


## SECTION - B

81. One mole of an ideal gas at 350 K is in a 2.0 L vessel of thermally conducting walls, which are in contact with the surroundings. It undergoes isothermal reversible expansion from 2.0 L to 3.0 L against a constant pressure of 4 atm . The change in entropy of the surroundings (AS) is $\qquad$ J K ${ }^{-1}$ (Nearest integer) Given : $\mathrm{R}=8.314 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{Mol}^{-1}$.
82. The mass of $\mathrm{NH}_{3}$ produced when 131.8 kg of cyclohexanecarbaldehyde undergoes Tollen's test is $\qquad$ kg. (Nearest Integer)
Molar Mass of $\mathrm{C}=12 \mathrm{~g} / \mathrm{mol}$
$\mathrm{N}=14 \mathrm{~g} / \mathrm{mol}$
$\mathrm{O}=16 \mathrm{~g} / \mathrm{mol}$
83. In an oligopeptide named Alanylglycylphenyl alanyl isoleucine, the number of $\mathrm{sp}^{2}$ hybridised carbons is
$\qquad$
84. An analyst wants to convert. 1L $\mathrm{HC1}$ of $\mathrm{pH}=1$ to a solution of HC 1 of pH 2 . The volume of water needed to do this dilution is $\qquad$ mL . (Nearest Integer)
85. Three organic compounds A, B and C were allowed to run in thin layer chromatography using hexane and gave the following result (see figure). The Rf value of the most polar compound is $\qquad$ $\times 10^{-2}$

86. 80 mole percent of $\mathrm{MgCl}_{2}$ is dissociated in aqueous solution. The vapour pressure of 1.0 molal aqueous solution of $\mathrm{MgCl}_{2}$ at $38^{\circ} \mathrm{C}$ is $\qquad$ mm Hg . (Nearest integer)
Given : Vapour pressure of water at $38^{\circ} \mathrm{C}$ is 50 mm Hg
87. 



The value of x in compound ' D ' is
88. At 600 K , the root mean square $(\mathrm{rms})$ speed of gas $X$ (molar mass $=40$ ) is equal to the most probable speed of gas $Y$ at 90 K . The molar mass of the gas Y is $\qquad$ $\mathrm{g} \mathrm{mol}^{-1}$. (Nearest integer)
89. The reaction $2 \mathrm{NO}+\mathrm{Br}_{2} \rightarrow 2 \mathrm{NOBr}$ takes places through the mechanism given below :
$\mathrm{NO}+\mathrm{Br}_{2} \Leftrightarrow \mathrm{NOBr}_{2}$ (fast)
$\mathrm{NOBr}_{2}+\mathrm{NO} \rightarrow 2 \mathrm{NOBr}$ (slow)
The overall order of the reaction is $\qquad$
90. Values of work function $\left(\mathrm{W}_{0}\right)$ for a few metals are given below

| Metal | Li | Na | K | Mg | Cu | Ag |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{W}_{0} / \mathrm{eV}$ | 2.42 | 2.3 | 2.25 | 3.7 | 4.8 | 4.3 |

The number of metals which will show photoelectric effect when light of wavelength 400 nm falls on it is
$\qquad$
Given : $\mathrm{h}=6.6 \times 10^{-34} \mathrm{~J} \mathrm{~s}$
$\mathrm{c}=3 \times 10^{8} \mathrm{~m} \mathrm{~s}^{-1}$
$\mathrm{e}=1.6 \times 10^{-19} \mathrm{C}$


## 12-April-2023 (Morning Batch) : JEE Main Paper

ANSWER KEY

## Mathematics




| Single Choice Correct |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 61 | D | 62. | D | 63. | B | 64. | B | 65. | A |
| 66 | D | 67. | B | 68. | A | 69. | A | 70. | B |
| 71 | A | 72. | A | 73. | A | 74. | D | 75. | A |
| 76 | C | 77. | B | 78. | C | 79. | A | 80. | D |
| Numerical Value |  |  |  |  |  |  |  |  |  |
| 81 | 3 |  | 60 | 83. | 10 | 84. | 9000 | 85. | 25 |
| 86 | 48 | 87. | 15 | 88. | 4 | 89. | 3 | 90. | 3 |

